**ORIGINAL ARTICLE** 



# Pumping power and heating area dependence of thermal resistance for a large-scale microchannel heat sink under extremely high heat flux

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## Abstract

In this paper, based on the Li-Peterson pumping consumption-thermal resistance optimization model, a single-phase structureoptimized large-scale microchannel heat sink with each channel having 0.2 mm width and 0.8 mm height for extremely high heat flux cooling was proposed and investigated. Employing deionized water as coolant, two different heat source areas were designed and the results were compared under different pumping power from 0.1 W to 6.5 W. The experimental and simulation results indicates that the proposed copper-based microchannel thermal management system can dissipate heat flux of 1000 W/cm<sup>2</sup> over 1cm<sup>2</sup> and 500 W/cm<sup>2</sup> over 5cm<sup>2</sup>, respectively, adding critical data support to the database of single-phase microchannel heat sink with heat removal capacity exceeding 1000 W/cm<sup>2</sup>. Moreover, the possible minimum thermal resistance over a broad pumping power range of 0.1 W to 6.5 W was explored. Extremely low thermal resistance of 0.065 K/W and 0.019 K/W were obtained for these two heating area scenarios. Overall, the proposed copper-based optimized microchannel heat sink is an ideal solution to cool high heat flux devices.

## Nomenclature

$A_{ch}$ Effective heat transfer area (	$(m^2)$ $c_p$	Specific heat capacity (J/(kg•K))
$A_{hs}$ Source dimension (m <sup>2</sup> )	$\dot{D}_h$	The characteristic dimension of microchannel (m)
Highlights	D <sub>tube</sub>	The inner diameter of tube (m)
• A structure-optimized large microchannel hea	at sink for $f$	Fanning friction factor
extremely high heat flux was designed.	$f_{app}$	Apparent friction factor
• Rough surface promotes heat transfer through	creating flow $G$	Flow rate (L/h)
<ul> <li>Actual heat fluxes of 1104.54W/cm<sup>2</sup> and 480.4 dissinated over 1 cm<sup>2</sup> and 5 cm<sup>2</sup> area</li> </ul>	60W/cm <sup>2</sup> were $h$	Convective heat transfer coefficient (W/ (m <sup>2</sup> •K))
<ul> <li>Dependence of thermal resistance on pumping</li> </ul>	g power between H	Height of channel (mm)
<ul> <li>0.1W and 6.5W was identified.</li> <li>Unprecedented low thermal resistance of 0.065K/W and 0.019K/W were obtained respectively.</li> </ul>		Thickness of microchannel substrate (mm)
		Current (A)
		Thermal conductivity of deionized water (W/
□ Ji Li		(m•K))
jili@ucas.ac.cn	L	Length of channel (mm)
<sup>1</sup> School of Engineering Science, University of Chinese Academy of Sciences, 19A Yu-quan-lu Road, Shijingshan District, Beijing 100049, PR China	m m	Mass flow (kg/s)
	of Chinese $N$	Number of microchannels
	Nu Nu	Nusselt number
School of Machanical Engineering Shanyang University	ng University P	Pressure (kPa)
of Technology, Shenyang 110870, China	$P_w$	Pumping power (W)
<sup>3</sup> Downing Information Industry Co. LTD P.	aijing China $P_{O}$	Input heating power by AC power (W)
Dawning mormation mousely Co., LTD, B	$\Delta P$	Pressure drop (kPa)
<ul> <li>Laboratory of Advanced Thermal Managem</li> <li>Tasknala size. School of Engineering Science</li> </ul>	nent Pr	Prandt number
of Chinese Academy of Sciences, 19A Yu-q	juan-lu Road, Q	Heating power (W)

Shijingshan District, Beijing 100049, PR China

q	Heat flux (W/cm <sup>2</sup> )
R	Total thermal resistance of heat sink (K/W)
$R_{cd}$	Conduction thermal resistance of heat sink
	(K/W)
$R_{cv}$	Convection thermal resistance of heat sink
	(K/W)
$R_c$	Capacity thermal resistance of heat sink
	(K/W)
Re	Reynolds number
Т	Temperature (°C)
$T_{hs}$	Junction temperature of heat sink (°C)
$T_m$	Mean temperature (°C)
$T_a$	Ambient temperature (°C)
$\Delta T$	Temperature difference (°C)
U	Voltage (V)
и	Velocity (m/s)
W	Width of channel (mm)
μ	Viscosity (kg/(m•s))
ρ	Density (kg/m <sup>3</sup> )
MEMS	Micro electro mechanical systems
DC	Direct current
AC	Alternating current
ch	Microchannel
hs	Heat sink
in/inlet	Inlet
out/outlet	Outlet

# 1 Introduction

The heat fluxes of devices such as high-performance computer chips, lasers and nuclear reactor are rapidly increasing, and the problem of heat accumulation and overheating is getting deteriorate [1]. In recent decades, the heat flux of the chip has reached 500 W/cm<sup>2</sup> in the field of Micro-Electro-Mechanical Systems (MEMS), and the local hot spot can exceed 1000 W/cm<sup>2</sup> [2–5]. For instance, the thermal flux of the next generation of IGBT modules will gradually increase from 100 W/cm<sup>2</sup> to 500 W/cm<sup>2</sup> [6]. For high-power laser devices, each diode laser needs to dissipate 500 W/cm<sup>2</sup> of heat flux while keeping the operating temperature as low as possible [7]. In the nuclear power engineering, the heat flux generated by components included in fusion reactors and defense applications can be up to 10<sup>4</sup> W/cm<sup>2</sup> [8].

Generally, the operating temperature of electronic devices should be less than 85 °C, and the reliability of products will be decreased by 50% if over-heated temperature exceeding 10 °C [9–11]. Since the demand of miniaturized design also limits the heat dissipation space, the uneven internal temperature distribution and poor heat dissipation have a series of negative effects, which will ultimately affect the performance and reliability of electronic devices. Therefore, reasonable thermal management is critical to electronic products [12, 13].

Current cooling technologies mainly include air cooling, liquid cooling, heat pipe, micro structure and spray cooling. As proposed by previous works, the traditional cooling method has relatively limited heat dissipation capacity, while the microchannel liquid cooling can handle a heat dissipation load of more than 1000 W/cm<sup>2</sup> [14–16], which is expected to meet the urgently demand for high heat flux cooling in the near future.

The concept of microchannel cooling technology was first introduced in the previous experimental study of Tuckerman and Pease in 1980s [17]. Due to micrometer size and large surface area to volume ratio, efficiently heat transfer can be obtained and the heat flux of 790 W/cm<sup>2</sup> was dissipated. Since then, owing to unique features of microchannel [18], the flow and heat transfer characteristics of microchannel under high heat flux have been extensively explored.

Skidmore et al. [19] proposed a laser diode array cooled by silicon monolithic microchannel. Up to 1.5 kW/cm<sup>2</sup> is achieved continuous wave at an emission wavelength of ~808 nm, and the continuous wave thermal resistance of the 10 bar diode array is 0.032 °C/W. Qu and Mudawar [20] investigated the pressure drop and heat transfer characteristics of a single-phase microchannel heat sink both experimentally and numerically. Using rectangular microchannel, the maximum heat flux dissipated in the experiment was 200 W/cm<sup>2</sup> with 86 kPa. Chang et al. [21] designed and tested a microchannel heat exchanger fabricated directly on the back of the chip. The results showed that under nonuniform heating conditions, microchannel with a width of 61 µm and a depth of 272 µm could obtain the best thermal resistance of  $0.09(K \cdot cm^2)/W$  and sustain the highest heat flux of 1250 W/cm<sup>2</sup>. In order to evaluate the practical application potential of mini/micro-channel radiators for high heat flux cooling, two samples of mini/micro-channel cooling loop were established and tested by Hirshfeld et al. [22]. The results showed that both structures could achieve high heat flux in the range of 500 W/cm<sup>2</sup>. Solovitz et al. [23] conducted experiments to study the trapezoidal copper microchannel heat sink for cooling high-power equipment. The thermal resistance of the cooler was  $0.15(K \cdot cm^2/W)$ , and the thermal performance was better than existing radiator. Brunschwiler et al. [24] tested the ability of parallel plates, microchannels, needle fins, linear and staggered structures to dissipate heat from a  $1 \text{ cm}^2$  chip heat source area. Using straight pin fins, with 200  $\mu$ m and 100  $\mu$ m pitch and 100  $\mu$ m and 200 µm height, cooler could remove heat flux of 177 W/ cm<sup>2</sup> and 186 W/cm<sup>2</sup>, respectively. A high-performance ultrathin manifold heat sink composed of jet and microchannel was proposed by Escher et al. [25]. With the hydraulic diameter of 35-80 µm, the microchannel heat sink proposed by

Koyuncuoğlu et al. [26] was able to absorb 127 W/cm<sup>2</sup> heat flux from hot spot and 50 W/cm<sup>2</sup> from the remaining heated surface. The microchannel cooler proposed by Kozłowska et al. [27] was able to cooling high power diode laser arrays at heat flux range from 200 W/cm<sup>2</sup> to 380 W/cm<sup>2</sup>.

In addition, many methods for enhancing flow and heat transfer in microchannel heat sinks have been further discussed [28–36]. Colgan et al. [28] described a practical implementation of micro-channel cooler with staggered and continuous fins designed for cooling ultra-high power chips such as microprocessors. Coolers of this design achieved chip cooling with power densities of 400 W/cm<sup>2</sup> and kept fluid pressure drop less than 35 kPa. Lee et al. [29] applied oblique fin microchannel heat sinks to alleviate the hot spots generated on the silicon chip with heat flux of 400 W/cm<sup>2</sup>, which effectively improved the temperature uniformity of the chip. Xia et al. [30] studied the characteristics of temperature variation and pressure drop in the compound corrugated microchannel radiator by experiment, in which the maximum heat flux was 200 W/cm<sup>2</sup>. Both Liu et al. [31] and Zhang et al. [32] used galinstan as cooling fluid exploring the heat transfer potential in minichannel and T-Y-type microchannel respectively, with maximum heat flux of 140 W/cm<sup>2</sup> and 300 W/cm<sup>2</sup>. Shamim et al. [33] proposed a scheme using microchannel to cooling 3D multicore chips, and studied it from three aspects: pressure drop, flow rate and heat transfer efficiency. With 0.05 W pumping power of the system, the heat dissipation of 200 W/cm<sup>2</sup> has been demonstrated. Xie et al. [34] investigated the pressure drop and heat transfer features of a microchannel applying staggered diamond micro-pin fins. Using visualization experiments, the mechanism of heat transfer were discussed. Yang et al. [35] proposed a novel optimization approach and a hybrid design using manifold arrangement and secondary channels for microchannel heat sink. The results indicate that the hybrid heat sink can simultaneously reduce the thermal resistance and pressure drop. More recently, Erp et al. [36] produced a monolithically integrated manifold microchannel cooling structure which withstands heat fluxes exceeding 1700 W/cm<sup>2</sup> using only 0.57 W/cm<sup>2</sup> of pumping power.

From relevant experimental studies mentioned above, it is evident that single-phase microchannel structures have great heat transfer potential which worthy of further exploring. From historical literature review, it is found that: (i) the experimental studies of single-phase microchannel cooling which heat flux exceeding 1000 W/cm<sup>2</sup> are very limited and the heat source is generally less than 1cm<sup>2</sup>, which cannot meet the large heating area and ultra-high heat flux demands, such as, IGBT and nuclear fusion facilities [37]; (ii) the thermal resistance under different pumping power conditions has not been well addressed, especially under high pumping power; (iii) before taking the ways to reduce the pressure drop along the microchannel heat sink (e.g., using manifold structures), the possible potential of microchannel heat sinks has not yet been identified, especially adopting the optimization of the structure.

The purpose of this study is to explore the heat transfer potential of a large-scale microchannel heat sink with an optimized structure based on our early established model of minimization of thermal resistance versus pump power under different conditions of high heat flux, heat area, and pumping power. Considering the comprehensive influence of pump power, heating area, and heat flux density on the thermal resistance of microchannel heat sinks, there are still lacking of such kind of historical work according to the author's knowledge. The ultimate the goal of our research on large-scale microchannel heat sinks is to provide practical and efficient cooling methods for large-scale and high heat flux equipment, such as high-power laser arrays and nuclear fusion reactors.

In this work, based on the Li-Peterson pumping power consumption-thermal resistance minimization model [38, 39], a large-scale microchannel heat sink is designed and fabricated with microchannel dimensions close to its optimized structure, of which rough surface was created along the microchannels through micromachining and etching process. The temperature variations and pressure drop along the single-phase microchannel heat sink were carefully measured and compared with the numerical simulation of turbulent heat transfer model. Two kinds of heat source areas  $(1 \text{ cm}^2 \text{ and } 5 \text{ cm}^2)$  are selected to study the hydraulics and thermal characteristics of microchannel heat sink with extremely high heat flux more than 500 W/cm<sup>2</sup> over 5cm<sup>2</sup> and 1000 W/cm<sup>2</sup> over 1cm<sup>2</sup> under very wide range of pumping power from 0.1 W-6.5 W, which was not revealed and compared before according to the authors' knowledge. The experimental results add critical data support to the database of single-phase microchannel heat sink with heat removal capacity exceeding 1000 W/cm<sup>2</sup> and explored the possible lowest thermal resistance over a broad pumping power range of 0.1 to 6.5 W.

## 2 Experimental apparatus

#### 2.1 Heat sink fabrication and assembly

The experimental device diagram of a high-power cooling cycle system is shown in the Fig. 1(a). The cooling system is divided into three parts: the water circulation system, the data collection system and the test section.

The water circulation system consists of thermostatic water tank, miniature water pump, filter, electronic flowmeter, valve, liquid-to-air heat exchanger, and fans. The electronic flow meter with a measurement range of  $0.1-0.6m^3/h$  and an accuracy of 0.5% was used to measure the real-time



(b) The locations of the pressure and temperature sensors on the microchannel heat sink.

volume flow of the circulating system. The deionized water subsequently entered the test section. After heated, the hot water flowed out of the heat sink and entered the liquid-to-air heat radiators. Eight 120 mm fans (each with a rated voltage of 12 V) were used to cool the radiators. Finally, the coolant returned to the tank and the inlet water temperature maintained at 25 oC. During the whole testing, the ambient temperature was maintained at about  $25 \pm 1$  °C.

The data acquisition system included pressure sensors, thermocouples, an Agilent data acquisition system and a

computer. Pressure sensors were arranged on both sides of the microchannel heat sink to measure the inlet and outlet pressure of the test section. The range of pressure sensor are  $0 \sim 5PSIG$  and  $0 \sim 50PSIG$  (OMEGA PX409-005 and PX409-050), and the measurement accuracy is 0.08%. As shown in the Fig. 1(b), two armored T-type thermocouples were installed at the inlet and outlet of heat sink to measure the change of coolant temperature. In addition, shown in Fig. 2, three T-type thermocouples were installed at different positions of the microchannel heat sink.  $T_{top}$  was located

Fig. 1 Schematic diagram of the experimental setup

at the center point of the upper cover, the  $T_{left}$  and  $T_{right}$  were 5 mm away from the center of the base plate.  $T_{hs}$  was located at the center point of the top surface of the heating block. The accuracy of OMEGA T-type thermocouples are  $\pm 0.2$  °C. All data were collected by the data acquisition instrument (Agilent 34970A with a measurement error of  $\pm 0.1$  °C).

The test section consists of a microchannel heat sink, a heating block and AC power supplies. During the experiment, the power input for the heating block was controlled by adjusting the AC power supplies. The heating block consists of two parts: the copper block and the cartridge heaters (each cartridge heater has a diameter of 10 mm, a length of 80 mm, and a rated power of 300 W). The copper block welded with the cartridge heaters was served as the heat source, and the total power of 10 cartridge heaters can reach 3000 W. To minimize the contact thermal resistance, the bottom surface of the heat sink substrate was tightly connected with the heating block by a thin layer tin soldering to fill the air gap. Stainless steel plates and bolts were used to fasten the test section. Two heating area cases were designed, as shown in Fig. 2, which were  $10 \text{ mm} \times 10 \text{ mm}$ and 50 mm  $\times$  10 mm, respectively. In order to minimize the heat loss from the surface of test section to the ambient, a layer of insulation cotton (thermal conductivity about  $0.032 \text{ W/(m \cdot K)}$  at 25 °C) with 6 mm thick was used to wrap the surface of test piece.

The microchannel heat sink with each channel having 200 microns width and 800 microns height was fabricated. Furthermore, scanning electron micrographs (SEM) of the microchannels are also shown in Fig. 3. A high voltage wire cutting process as selected as the processing method in this work, other than etching or skiving fabrication. The purpose of high voltage wire cutting is to generate very rough inner surface to produce small perturbation in microchannel flow under comparatively low Reynolds number. After machining process, the

microchannel heat sink was further developed in high concentration hydrochloric acid. Such an extra corrosion process is to increase the roughness of the microchannel surface. The typical roughness from Fig. 3 can be determined around 5 microns ~ 10 microns. This roughness cannot be ignored compared to 200 microns channel width.

## 3 Data processing and analysis

## 3.1 Flow Characteristics

The pressure drop in microchannel associated with apparent friction factor  $f_{app}$  can be expressed as

$$\Delta P_{ch} = \frac{2f_{app}\rho u_{ch}^2 L}{D_h} \tag{1}$$

where L is the length of microchannel;  $D_h$  is the hydraulic diameter, expressed as followed:

$$D_h = \frac{4WH}{2(W+H)} \tag{2}$$

where W is the width of microchannel, and H is the height of microchannel.

In the experimental process, the velocity can be calculated by measuring the flow rate, so the friction coefficient can be calculated by measuring the pressure drop and flow rate. At the same time, according to the definition of Reynolds number, the relationship between friction coefficient and Reynolds number can be further discussed,

$$Re = \frac{u_{ch}D_h}{v}$$
(3)





Fig. 3 SEM pictures and schematic diagram of microchannels



(a) Top view of the passage



(c) Rough surface of the microchannel



(b) Eagle view



(d) Schematic diagram of heat sink

$$\operatorname{Re} = \frac{u_{ch}D_h}{v}$$

where v is the kinematic viscosity. In the calculation process, the thermo-physical parameters such as the density and dynamic viscosity coefficient of the fluid are calculated based on  $T_m$  which is expressed as following:

$$T_m = \frac{T_{in} + T_{out}}{2} \tag{4}$$

Where  $T_{in}$  and  $T_{out}$  are the temperature of inlet and outlet.

# 3.2 Heat Transfer

The analysis of heat transfer characteristics of microchannels is mainly focused on the study of convective heat transfer coefficient and Nu number. When the fluid passes through the microchannel, the heat transferred by the heating block was obtained. Electrical heating power was controlled by adjusting the voltage of AC power supply. The formula for calculating heating power is as follow,

$$P_0 = U \cdot I \tag{5}$$

The formula for heat transfer by coolant is as follow

$$Q = c_p m \Delta T \tag{6}$$

Where  $P_Q$  is heating power, U is voltage of AC power supply, I is current of AC power supply,  $c_p$  is specific heat capacity of water, m is mass flow of water,  $\Delta T$  is temperature difference

between import and export water. In the absence of heat loss, the results from Eq. (5) and (6) should be same.

The effective heat transfer coefficient h is expressed as

$$h = \frac{Q}{A_{ch} \cdot (T_{hs} - T_m)} \tag{7}$$

where Q is the real input heat load from Eq. (6);  $A_{ch}$  is effective heat transfer area of the microchannel heat sink as following:

$$A_{ch} = (2HL_{heat} + 2WL_{heat}) \cdot N \tag{8}$$

where *W* and *H* are the width and height of microchannels;  $L_{heat}$  is the length of the microchannel involved in heat transfer; *N* is the number of channel to be heated.

Nusselt number can be calculated as:

$$Nu = \frac{hD_h}{k_w} \tag{9}$$

where  $k_w$  is the thermal conductivity of deionized water.

#### 3.3 Thermal performance

The total thermal resistance of heat sink *R* was divided into three components: conduction thermal resistance  $R_{cd}$  convection thermal resistance,  $R_{cy}$  and capacity thermal resistance  $R_{cy}$ 

$$R = R_{cd} + R_{cv} + R_c \tag{10}$$

$$R = \frac{T_{hs} - T_{in}}{Q} \tag{11}$$

$$R_{cd} = \frac{H_b}{k_{cu}A_{hs}} \tag{12}$$

$$R_{cv} = \frac{T_{hs} - T_m}{Q} - R_{cd} = \frac{1}{hA_{hs}}$$
(13)

$$R_c = \frac{T_m - T_{in}}{Q} \tag{14}$$

where  $H_b$  is the thickness of microchannel substrate,  $k_{cu}$  is the thermal conductivity of copper, and  $A_{hs}$  is the area of heat source.

## 3.4 Uncertainty analysis

Uncertainty analysis for each parameter is summarized in Tab. 1, respectively:

# 4 Turbulent heat transfer model of microchannel heat sink

The computational domain according to the experimental microchannel heat sink is shown in Fig. 4. The pressure sensors arranged on inlet and outlet of the microchannel heat sink were ignored to simplify the model.

The three dimensional turbulent flow and heat transfer processes were numerically solved with the following assumptions: (1) the heat transfer fluid is single phase, Newtonian and incompressible; (2) both fluid flow and heat transfer are in steady state; (3) the radiation heat transfer, body force and dissipating heat caused by viscosity are neglected. According to the above assumptions, the governing equations of continuity, momentum and energy for liquid can be established as follows.



Fig. 4 Computational domain of the microchannel heat sink

Continuity equation:

$$\frac{\partial(\rho u)}{\partial x} + \frac{\partial(\rho v)}{\partial y} + \frac{\partial(\rho w)}{\partial z} = 0$$

Momentum equation:

(

$$\frac{\partial(\rho uu)}{\partial x} + \frac{\partial(\rho uv)}{\partial y} + \frac{\partial(\rho uw)}{\partial z} = -\frac{\partial P}{\partial x} + \frac{\partial}{\partial x} \left[ \left(\mu + \mu_t\right) \left(\frac{\partial u}{\partial x} + \frac{\partial u}{\partial x}\right) \right] \\ + \frac{\partial}{\partial y} \left[ \left(\mu + \mu_t\right) \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x}\right) \right] + \frac{\partial}{\partial z} \left[ \left(\mu + \mu_t\right) \left(\frac{\partial u}{\partial z} + \frac{\partial w}{\partial x}\right) \right]$$

$$\frac{\partial(\rho v u)}{\partial x} + \frac{\partial(\rho v v)}{\partial y} + \frac{\partial(\rho v w)}{\partial z} = -\frac{\partial P}{\partial y} + \frac{\partial}{\partial x} \left[ \left(\mu + \mu_t\right) \left(\frac{\partial v}{\partial x} + \frac{\partial u}{\partial y}\right) \right] \\ + \frac{\partial}{\partial y} \left[ \left(\mu + \mu_t\right) \left(\frac{\partial v}{\partial y} + \frac{\partial v}{\partial y}\right) \right] + \frac{\partial}{\partial z} \left[ \left(\mu + \mu_t\right) \left(\frac{\partial v}{\partial z} + \frac{\partial w}{\partial y}\right) \right]$$

$$\frac{\partial(\rho w u)}{\partial x} + \frac{\partial(\rho w v)}{\partial y} + \frac{\partial(\rho w w)}{\partial z} = -\frac{\partial P}{\partial z} + \frac{\partial}{\partial x} \left[ \left( \mu + \mu_t \right) \left( \frac{\partial w}{\partial x} + \frac{\partial u}{\partial z} \right) \right] \\ + \frac{\partial}{\partial y} \left[ \left( \mu + \mu_t \right) \left( \frac{\partial w}{\partial y} + \frac{\partial v}{\partial z} \right) \right] + \frac{\partial}{\partial z} \left[ \left( \mu + \mu_t \right) \left( \frac{\partial w}{\partial z} + \frac{\partial w}{\partial z} \right) \right]$$

Energy equation for the fluid region:

Parameters	Formula	Maximum uncertainty
Т	_	±0.20 °C
Р	-	$\pm 0.08\%$
G	-	$\pm 0.5\%$
Re	$\frac{\triangle Re}{Re} = \sqrt{\left(\frac{\triangle u_m}{u_m}\right)^2 + \left(\frac{\triangle D_h}{D_h}\right) + \left(\frac{\triangle v}{v}\right)^2}$	$\pm 0.89\%$
h	$\frac{\triangle h}{h} = \sqrt{\left(\frac{\triangle Q}{Q}\right)^2 + \left(\frac{\triangle A_{ch}}{A_{ch}}\right) + \left(\frac{\triangle T_{hs}}{T_{hs}}\right)^2 + \left(\frac{\triangle T_m}{T_m}\right)^2}$	±5.63%
Nu	$\frac{\Delta Nu}{Nu} = \sqrt{\left(\frac{\Delta h}{h}\right)^2 + \left(\frac{\Delta D_h}{D_h}\right)^2 + \left(\frac{\Delta k_w}{k_w}\right)^2}$	±5.66%

Table 1The uncertainty ofmain parameters



(a) Heat source dimension: 10 mm×10 mm.

Fig. 5 Thermal balance of specimens

$$\frac{\partial(\rho uT)}{\partial x} + \frac{\partial(\rho vT)}{\partial y} + \frac{\partial(\rho wT)}{\partial z} = \frac{\partial}{\partial x} \left[ \left( \frac{\lambda_f}{c_p} + \frac{\mu_t}{\sigma_T} \right) \frac{\partial T}{\partial x} \right] \\ + \frac{\partial}{\partial y} \left[ \left( \frac{\lambda_f}{c_p} + \frac{\mu_t}{\sigma_T} \right) \frac{\partial T}{\partial y} \right] + \frac{\partial}{\partial z} \left[ \left( \frac{\lambda_f}{c_p} + \frac{\mu_t}{\sigma_T} \right) \frac{\partial T}{\partial z} \right]$$
(15)

Energy equation for the solid region:

$$\frac{\partial}{\partial x} \left( \lambda_s \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left( \lambda_s \frac{\partial T}{\partial y} \right) + \frac{\partial}{\partial z} \left( \lambda_s \frac{\partial T}{\partial z} \right) = 0 \tag{16}$$

In this study, the standard k- $\varepsilon$  turbulence model was used to simulate the turbulent heat transfer. The governing equations of turbulence are given as follows.

$$\frac{\partial(\rho uk)}{\partial x} + \frac{\partial(\rho vk)}{\partial y} + \frac{\partial(\rho wk)}{\partial z} = \frac{\partial}{\partial x} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x} \right] \\ + \frac{\partial}{\partial y} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial y} \right] + \frac{\partial}{\partial z} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial z} \right] + G_k - \rho \epsilon$$

$$\frac{\partial(\rho u\varepsilon)}{\partial x} + \frac{\partial(\rho v\varepsilon)}{\partial y} + \frac{\partial(\rho w\varepsilon)}{\partial z} = \frac{\partial}{\partial x} \left[ \left( \mu + \frac{\mu_t}{\sigma_{\varepsilon}} \right) \frac{\partial \varepsilon}{\partial x} \right] \\ + \frac{\partial}{\partial y} \left[ \left( \mu + \frac{\mu_t}{\sigma_{\varepsilon}} \right) \frac{\partial \varepsilon}{\partial y} \right] + \frac{\partial}{\partial z} \left[ \left( \mu + \frac{\mu_t}{\sigma_{\varepsilon}} \right) \frac{\partial \varepsilon}{\partial z} \right] \\ + \frac{\varepsilon}{k} (c_1 G_k - c_2 \rho \varepsilon)$$

$$\mu_{t} = c_{\mu}\rho \frac{1}{\epsilon}$$

$$G_{k} = \mu_{t} \left\{ 2\left[ \left(\frac{\partial u}{\partial x}\right)^{2} + \left(\frac{\partial v}{\partial y}\right)^{2} + \left(\frac{\partial w}{\partial z}\right)^{2} \right] + \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x}\right)^{2} + \left(\frac{\partial u}{\partial z} + \frac{\partial w}{\partial x}\right)^{2} + \left(\frac{\partial v}{\partial z} + \frac{\partial w}{\partial y}\right)^{2} \right\}$$
(17)

 $k^2$ 



(b) Heat source dimension:  $50 \text{ mm} \times 10 \text{ mm}$ .



Fig. 6 Comparison of experimental results with numerical simulations of the junction temperature change with heat flux at different flow rates

where  $\lambda$  *is* the thermal conductivity,  $\mu_t$  represents the turbulent viscosity,  $c_{\mu}$ ,  $c_1$ ,  $c_2$ ,  $\sigma_k$ ,  $\sigma_e$  and  $\sigma_T$  equal to 0.09, 1.44, 1.92, 1.0, 1.3 and 0.9, respectively.

The meshing tool GAMBIT was used to mesh the computational domain of the microchannel heat sink, and computational fluid dynamics (CFD) software Fluent was used to solve the fluid flow and heat transfer numerically in the microchannel heat sink [40]. The momentum and energy conservation equations were discredited by a second-order upwind scheme. The SIMPLEC algorithm was adopted to deal with the relationship between velocity and pressure. The computations were considered to be converged when the



(a)Source dimension: 10mm×10mm.



(b) Source dimension: 50mm×10mm

Fig. 7 Temperature clouds at the surface of the microchannel base plate

convergence residuals are less than  $10^{-4}$  for the continuity and momentum equations and  $10^{-6}$  for the energy equation.

The inlet was set as the velocity inlet, and the temperature was kept at 298.15 K. The outlet was set as pressure outlet and the relative pressure is 0 Pa. In addition, a heat source with a constant heat flux was applied to the bottom of the microchannel heat sink, as shown in Fig. 2, and the other walls were assumed to be thermally insulated. Copper with thermal conductivity of 387.6 W/(m•K) was chosen as the material for the microchannel heat sink, and liquid water with temperature dependent thermophysical properties [41] was used as the heat transfer fluid.

The grid independence study was carried out based on the microchannel heat sink model with three grid densities (1,205,151 cells, 2,671,119 cells and 3,586,719 cells). The deviations in  $\Delta P$  and  $T_{hs}$  between the 2,671,119 cells and 3,586,719 cells are 0.33% and 0.12%, respectively. This indicates that the calculation with grid densities of 2,671,119 cells is accurate enough. Therefore, all the computations were carried out using the mesh with 2,671,119 cells considering both computational accuracy and efficiency.

# 5 Experiment results and discussion

### 5.1 Energy balance calibration

As shown in the Fig. 5(a), (b), the heat input from the AC power supply was compared with the heat carried away by the coolant water. The value calculated by Eq. (6) is lower

ment error of temperature and flow rate; the second part of the thermal leakage, which occupied the main part, is caused by convection and radiant heat transfer on the surface of the heating block. During the experiment, as the input power increased, a large temperature gradient was generated on the surface of the heating block. For example, when the input power of the AC power supply was 1000 W, the maximum temperature of the copper block surface can reach 500 °C, which exceeded the melting point of the thermal insulation cotton. Insulation material will deform and produce large amounts of fumes when overheated, which is detrimental to the proper functioning of the heat source.

than that of the power input of AC power supply from

Eq. (5), indicating that there exists heat loss. As the input

heat increased from 100 to 1300 W and 3000 W respec-

tively, this deviation became more obvious, ranging from 10 to 30%. According to Eq. (6), the highest heat flux values

achieved in the experiments were actually 1104.54 W/cm<sup>2</sup>

and 480.60 W/cm<sup>2</sup> for the heat source areas of 1cm<sup>2</sup> and

5cm<sup>2</sup>, respectively. The heat loss is mainly composed of two

parts: the first part is the heat loss caused by the measure-

The junction temperature  $T_{hs}$  of the heating source at different flow rate are plotted against heat fluxes in Fig. 6(a) ,(b), respectively. In Fig. 6(a), it is showed that the temperature increased linearly with the input heat flux increasing from 100 W/cm<sup>2</sup> to 1300 W/cm<sup>2</sup> with heat source dimension of 1cm<sup>2</sup>. Taking 85 °C as the upper limit of junction





Fig. 8 Temperature cloud plots of cross sections in the length direction (y direction) for two heat source areas

temperature for normal operation of electronic equipment, the structure proposed in this paper dissipated heat flux greater than 1000 W/cm<sup>2</sup> at the flow rate of 200L/h, which means that the suggested heat sink can realize the thermal management of heat flux of 1000 W/cm<sup>2</sup> without overheating.

In addition, it can be seen from the Fig. 6(a) that under the same heat load, the  $T_{hs}$  decreased as the flow rate increased, especially at high heat flux. With a gradual increased in flow rate from 50L/h to 200L/h, the junction temperature was 109.20 °C, 94.85 °C, 89.90 °C and 87.15 °C at the heat flux of 1000 W/cm<sup>2</sup>, and the temperature decrease ratio was 13.14%, 5.22% and 3.06%, respectively.

Figure 6(a) also exhibits the comparison between the experimental results and numerical simulations of the junction temperature variation with heat flux. It can be seen from the figure that the trend of temperature change is almost the same. At smaller flow rates that below 100 L/h, a large difference occurred when the heat flux exceeded 700 W/cm<sup>2</sup>.



(b) Source dimension: 50mm×10mm

Fig. 9 Comparison of experimental and numerical simulation results regarding the pressure drop of heat sink

This may be due to the unavoidable leakage of heat from the heating block during the experiment making the actual input heat density lower than the uniform heat flux in the simulation. From the temperature cloud diagram of the microchannel base plate as given in Fig. 7(a), it can be observed that at higher heat flux, the temperature of the heat source region will gradually decrease along the flow direction as the flow rate increases. However, during the experiment, the junction temperature was measured at the top of the heating block, and there was a thin layer of solder paste between the microchannel heat sink base plate and the heating block. This means that there was an additional thermal resistance between the temperature measurement point and the heat sink base plate, which slightly weaken the heat transfer. In addition, as can be seen in Fig. 8(a) the heat flux was uniformly input during the simulation and the effect of solder paste on heat transfer was not considered. Therefore, at high flow rates, the simulation results of junction temperature are lower than the experimental results.

Variations of the junction temperature with heat flux for the heating source of  $5\text{cm}^2$  are shown in Fig. 6(b). At a constant flow rate, the junction temperature increased linearly with the increases in heat flux. When the input heat flux increased from 100 W/cm<sup>2</sup> to 600 W/cm<sup>2</sup>, the junction temperature rose from 38.57 °C to 93.33 °C at the flow rate of 100L/h. Also, under all operating conditions, the  $T_{hs}$  was less than 100 °C. When the flow rate gradually increased from 80L/h to 200L/h, the  $T_{hs}$  dropped significantly, and the decline slope was basically the same, about 6%. This result indicated that increasing the flow rate within the allowable range could reduce the overall temperature of the heat sink and enhance the heat transfer performance.



Fig. 10 Summary and comparison of the published experimental results and ours

	Pumping power (W)	1.84	0.15	0.28	0.73	00 0.30	0.48	-611 0.21	0.41	-750 0.1–6.5
	Re	NA	NA	NA	NA	< 10	NA	250-	2481	150-
	Thermal resistance (K/W)	0.0	0.22	0.078	0.05	0.17	0.022	0.446	0.034	0.065 and 0.019
	Heat source area (cm <sup>2</sup> )	1×1	$1 \times 1.3$	1.92	ε	1	2×2	$0.4 \times 0.6$	$0.22 \times 0.22$	1 and 5
	Heat flux (W/cm <sup>2</sup> )	181–790	1250	104	400	200	100	200	300	1104.54
	$\stackrel{T_{in}}{(^{\circ}C)}$	23	NA	20	22	25	20	25	27	25
	Flow rate (ml/min)	282–516	159	240	NA	<400	1300	75–190	1200–4800	833–3333
	Pressure drop (kPa)	213.745	< 57.7	< 68.95	< 35	< 70	22	< 65	8	< 133.48
	Coolant	Water	DI water	DI water	Water	DI water	Water	DI water	Galinstan	DI water
	Loop form	NA	Closed	Closed	Closed	NA	Closed	Closed	Closed	Closed
11 ·S1.1 m c	Material	Silicon	Silicon	Copper	Silicon	Silicon	Silicon	Silicon	Copper	Copper
	Channel types	Rectangular	Rectangular	Trapezoidal	Staggered and continuous fins	Rectangular pin fin	Rectangular	Straight and corrugated channel	Rectangular	Rectangular
dvo notietto	D <sub>h</sub> (µm)	85–95	100–225	NA	96, 106	182, 333	46–158	150, 240	1667	320
unparison u pur	Author	Tuckerman and Pease [17]	Chang et al. [21]	Solovitz et al. [23]	Colgan et al. [28]	Brunschwiler et al. [24]	Escher et al. [25]	Xia et al [30]	Zhang et al. [32]	
	Years	1981	2005	2006	2007	2008	2010	2015	2019	This paper

Table 2Comparison of published experimental results in Fig. 10

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Figure 6(b) also shows a comparison of the experimental and numerical results for junction temperature. Figures 7(b)and 8(b) shows the results of the numerical simulation of the temperature cloud plots. As can be seen from the figure, the values of the experimental results are higher than those of the simulations, and the deviation of the temperature increases with the increase of the heat flux. The reason for this phenomenon may be that the uneven solder paste used to connect the heat sink to the heating block caused a large resistance to heat transfer, especially at large heat source areas. In addition, the uniform heat flux was used as a heat source boundary condition in the numerical simulations and the effect of the solder paste on the heat transfer was not taken into account. If we adjust the thickness of the solder in the model, this discrepancy will be reduced. It can be predicted from the simulation results that the microchannel heat sink proposed in this paper can achieve better cooling performance at high heat flux and large heat transfer area if the influence of contact thermal resistance can be reduced.

The pressure drop of microchannel heat sink versus Re number under different heat flux are illustrated in Fig. 9(a) and (b). As can be seen from the Fig. 9(a), the pressure drop of the heat sink and its rising rate increased with Reynolds number under the experimental conditions. The largest pressure drop of 133.48 kPa was recorded at q = 1200 W/cm<sup>2</sup> and Re = 667. In addition, for the same number of Re, the pressure drop had a slight fluctuation with the increase in heat flux. This may due to the fact that the viscosity of the water was strongly influenced by temperature, and when the heat flux was increased, the water temperature became higher, the viscosity decreased, and Re increased, resulting in changes in the coefficient of friction and pressure drop.

In Fig. 9(b), since the main structure and the channel size of the heat sink for two heating source scenarios are the same, the pressure drop of heat sink is of the same order of magnitude. The overall trend was that the pressure drop increased with increasing of *Re*. The maximum value of pressure drop was 114.87 kPa when the q = 500 W/cm<sup>2</sup> and Re = 726.

Figure 9(a), (b) also compared the experimental and numerical results of microchannel pressure drop. As can be seen in the figures, there is some deviation between the two results and the experimental results are slightly larger than the simulated results. There are three possible reasons for this discrepancy: (1) this is a simplified model, as shown in Fig. 4, and the influence from some obstacles (e.g. sensors) was not considered; (2) the standard k- $\varepsilon$  turbulence model might not match the real situation perfectly; (3) the measurement errors of the pressure sensors will affect the results. During the simulation process, both the channel and the fluid were in the ideal state, so the simulation results were lower than the experimental results.

# 5.3 The relationship of thermal resistance and pumping power for two heating scenarios

Under the maximum input heat flux of  $1300 \text{ W/cm}^2$  and flow rate of 200L/h, the total thermal resistance was 0.065 K/W for 1cm<sup>2</sup> heat source. The lowest value of the thermal resistance was 0.019 K/W for 5cm<sup>2</sup> heat source at the input heat flux of 600 W/cm<sup>2</sup> and the flow rate of 200L/h. When the heat source area increased from 1cm<sup>2</sup> to 5cm<sup>2</sup>, the thermal resistance value decreased significantly, which is due to the lower input heat flux. When the unit is converted to K•cm<sup>2</sup>/W, the thermal resistance value of the two different heat transfer area is the consistent.

Figure 10 and Table 2 summarizes the comparison of some published experimental results for different heat source area, pumping power, and thermal resistance in the historic literature which were aiming at solving high heat flux, and the results in this work are also marked in the figure using red and blue dots. It is obvious from the diagram that the turbulence-enhanced and structure-optimized microchannel proposed in this paper achieves an unprecedented ultra-low thermal resistance for a large heat transfer area with a very high heat flux, consuming only 6 W of pumping power.

# 6 Conclusive remarks

In order to explore the heat transfer potential of microchannel heat sinks for high heat flux cooling, a structure-optimized microchannels, with 0.2 mm width, 0.8 mm height, were experimentally and numerically studied under different heat flux and flow rate. A carefully designed cooling circulation system has been proposed to meet the heat dissipation requirements of high heat flux. The inlet and outlet temperature, pressure drop and flow rate of coolant are measured under different heat loads in this work. The experimental and simulation result indicates that the proposed copper-based microchannel thermal management system can dissipate heat flux of 1000 W/cm<sup>2</sup> over 1 cm<sup>2</sup> and 500 W/cm<sup>2</sup> over 5 cm<sup>2</sup>, respectively. In addition, extremely low thermal resistance of 0.065 K/W and 0.019 K/W were obtained for these two heating area scenarios. Overall, the proposed copper-based optimized microchannel heat sink is a practical and efficient cooling method that promises to be used for large-scale and high heat flux equipment. In future work, modifications to the structure of proposed heat sink, such as a manifold layout or porous surface coating, can be considered to achieve heat dissipation with ultra-high heat flux.

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